

## In the Claims

1 1. (currently amended) A method for evaluating an error-correcting code for  
2 a data block of a finite size, comprising:

3 defining an error-correcting code by a parity check matrix;  
4 representing the parity check matrix as a bipartite graph; ~~and~~  
5 iteratively renormalizing a single node in the bipartite graph until a  
6 predetermined threshold is reached; and

7 wherein the bipartite graph includes variable nodes representing  
8 variable bits of the data block, and check nodes representing parity bits of  
9 the data block, and the renormalizing further comprises:

10 selecting a particular variable node as a target node;  
11 selecting a particular node to be renormalized;  
12 measuring a distance between the target node and every other  
13 node in the bipartite graph;

14 if there is at least one leaf variable node, renormalizing a  
15 particular leaf variable node farthest from the target node, otherwise

16 if there is at least one leaf check node, renormalizing a  
17 particular leaf check node farthest from the target node, otherwise

18 renormalizing a non-leaf variable node farthest from the target  
19 node and having fewest directly connected check nodes.

1 2. (original) The method of claim 1 wherein the predetermined threshold is a  
2 minimum number of remaining nodes.

1 3. (canceled)

1 4. (canceled)

1 5. (currently amended) The method of claim 1 wherein the bipartite graph is  
2 ~~loop-free~~ cycle-free.

1 6. (currently amended) The method of claim 1 wherein the bipartite graph  
2 includes at least one ~~loop~~ cycle.

1 7. (currently amended) The method of ~~claim 4~~ claim 1 wherein a  
2 transmission channel is a binary erasure channel, and further comprising:  
3       decorating the bipartite graph with numbers  $p_{ia}$  representing  
4 probabilities of messages from variable nodes to check nodes and with  
5 numbers  $q_{ai}$  representing probabilities of messages from check nodes to  
6 variable nodes, and the renormalizing of the non-leaf variable node further  
7 comprises:  
8       enumerating all check-nodes  $a$  which are connected to the non-leaf  
9 variable node;  
10       enumerating all other variable nodes  $j$  attached to the check nodes  $a$ ;  
11 and  
12       transforming the numbers  $q_{aj}$ .

1 8. (original) The method of claim 7 wherein the transforming of the numbers  
2  $q_{aj}$  further comprises:  
3       enumerating all check nodes and variable nodes out to a  
4 predetermined distance from the target node;

5       constructing a logical argument to determine combinations of erasure  
6       causing a particular message from the check node  $a$  to the variable node  $j$  to  
7       be an erasure;  
8       translating the logical argument into a transformation for the number  
9        $q_{aj}$ .

1    9. (currently amended) The method of claim 8 further comprising  
2    comprising:

3       terminating the renormalizing upon reaching the predetermined  
4       threshold by an exact determination.

1    10. (original) The method of claim 9 wherein the remaining bipartite graph  
2    includes  $N$  nodes in the exact determination, and further comprising:

3       converting the decorated graph with numbers  $q_{ai}$  and  $p_{ia}$  into an  
4       erasure graph with an erasure probability  $x_i$  with each node  $i$  of the bipartite  
5       graph;

6       generating all  $2^N$  possible messages; and

7       decoding each of the  $2^N$  messages using a belief propagation decoder,

8       where each message has a probability  $p = \prod x_i \prod (1 - x_j)$ .

1    ~~11. (currently amended) The method of claim 7 wherein all the numbers  $q_{ai}$~~   
2    ~~are initialized to zero, and~~

3    ~~all the numbers  $p_{ia}$  are initialized to an erasure rate of the transmission~~  
4    ~~channel.~~

5    The method of claim 7 wherein all the numbers  $q_{ai}$  are initialized to zero,  
6    and

7 all the numbers  $p_{ia}$  are initialized to an erasure rate of the transmission  
8 channel.

1 12. (original) The method of claim 7 further comprising:  
2 defining the error-correcting code by a generalized parity check  
3 matrix wherein columns represent variable bits and rows define parity bits,  
4 and wherein an overbar is placed above columns representing hidden  
5 variable bits which are not transmitted; and  
6 representing the hidden variable bits by hidden nodes in the bipartite  
7 graph.

1 13. (original) The method of claim 12 wherein the transmission channel is a  
2 binary erasure channel and wherein the error-correcting code is defined by a  
3 generalized parity check matrix, and further comprising:  
4 initializing the numbers  $p_{ia}$  for hidden nodes  $i$  to one.

1 14. (previously presented) The method of claim 7 wherein the transmission  
2 channel is an additive white Gaussian noise channel, and further comprising:  
3 representing messages between nodes in the bipartite graph by  
4 Gaussian distributions.

1 15. (currently amended) The method of claim 1, and further comprising:  
2 selecting a set of criterion by which to evaluate error-correcting codes;  
3 generating a plurality of error-correcting codes; and  
4 searching the plurality of error-correcting codes for an optimal error-  
5 correcting code according to the set of criterion.

1 16. (currently amended) The method of claim 15, and further comprising:  
2 evaluating an error rate for each error-correcting code at a plurality of  
3 nodes; and  
4 generating the optimal error-correcting code according to the  
5 evaluated error-rate.

1 17. (original) The method of claim 1 further comprising:  
2 evaluating an error rate for the renormalized bipartite graph.

1 18. (currently amended) A method for evaluating an error-correcting code  
2 for a data block of a finite size, comprising:  
3 defining an error-correcting code by a parity check matrix;  
4 representing the parity check matrix as a bipartite graph, wherein the  
5 bipartite graph includes variable nodes representing variable bits of the data  
6 block, and check nodes representing parity bits of the data block;  
7 iteratively renormalizing a single node in the bipartite graph until a  
8 predetermined threshold is reached, wherein the renormalizing further  
9 ~~comprises;~~ comprises:  
10 selecting a particular variable node as a target node; and  
11 selecting a particular node to be renormalized;  
12 measuring a distance between the target node and every other node in  
13 the bipartite graph;  
14 if there is at least one leaf variable node, renormalizing a particular  
15 leaf variable node farthest from the target node, otherwise  
16 if there is at least one leaf check node, renormalizing a particular leaf  
17 check node farthest from the target node, otherwise

renormalizing a non-leaf variable node farthest from the target node and having fewest directly connected check nodes;

wherein a transmission channel is a binary erasure channel, and further ~~comprising;~~ comprising:

decorating the bipartite graph with numbers  $p_{ia}$  representing probabilities of messages from variable nodes to check nodes and with numbers  $q_{ai}$  representing probabilities of messages from check nodes to variable nodes, and the renormalizing of the non-leaf variable node further comprises:

enumerating all check-nodes  $a$  which are connected to the non-leaf variable node;

enumerating all other variable nodes  $j$  attached to the check nodes  $a$ ;

wherein the enumerating further ~~comprises;~~ comprises:

enumerating all check nodes and variable nodes out to a predetermined distance from the target node;

constructing a logical argument to determine combinations of ~~erasure~~ erasures causing a particular message from the check node  $a$  to the variable node  $j$  to be an erasure;

translating the logical argument into a transformation for the number  $q_{aj}$ ; and

transforming the numbers  $q_{aj}$  numbers  $q_{aj}$ .